

On the effect of the seed population: a comparison of low energy boundaries in the BAS Radiation Belt Model

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Introduction

- Recent work has shown the importance of the seed population
- Captured in models by the low energy boundary condition

- Here we use different low energy boundary conditions in the BAS Radiation Belt Model
 1. Using POES MEPED data – two methods developed
 2. Using Van Allen Probes MagEIS data
 3. Using a Kp driven statistical method derived from CRRES data – see Glauert et al., 2014

- POES satellites operate in a polar orbit
- Orbit the Earth ~ 14 times each day
- Cross a range of L^*
- Rapid coverage of the radiation belt region
- >19 years of data
- Up to 5 POES satellites – multiple MLT planes
- Two main challenges:
 1. Integral flux data
 2. Low equatorial pitch angle

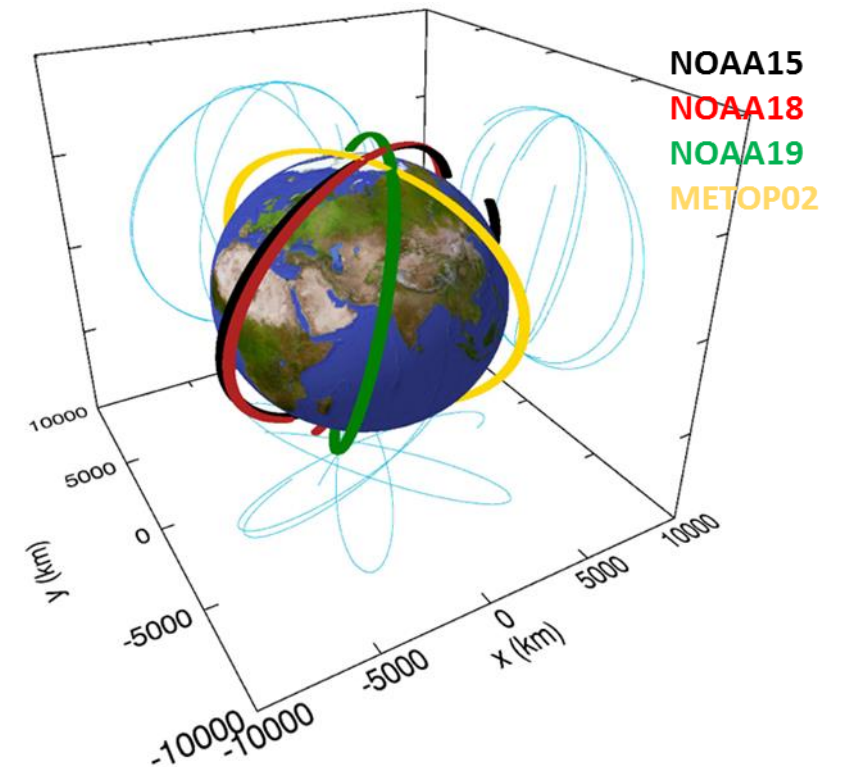
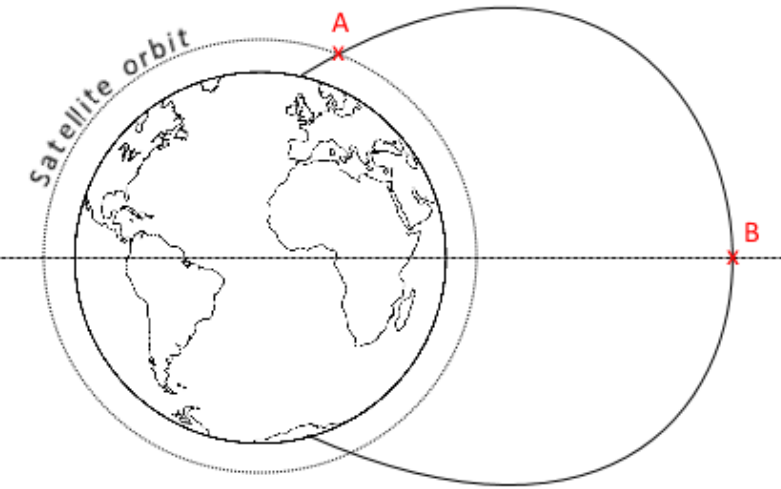


Figure 1 – Trajectories of all available POES satellites from 2014-06-22 23:00:00 to 2014-06-23 00:40:00

Convert to Omnidirectional flux

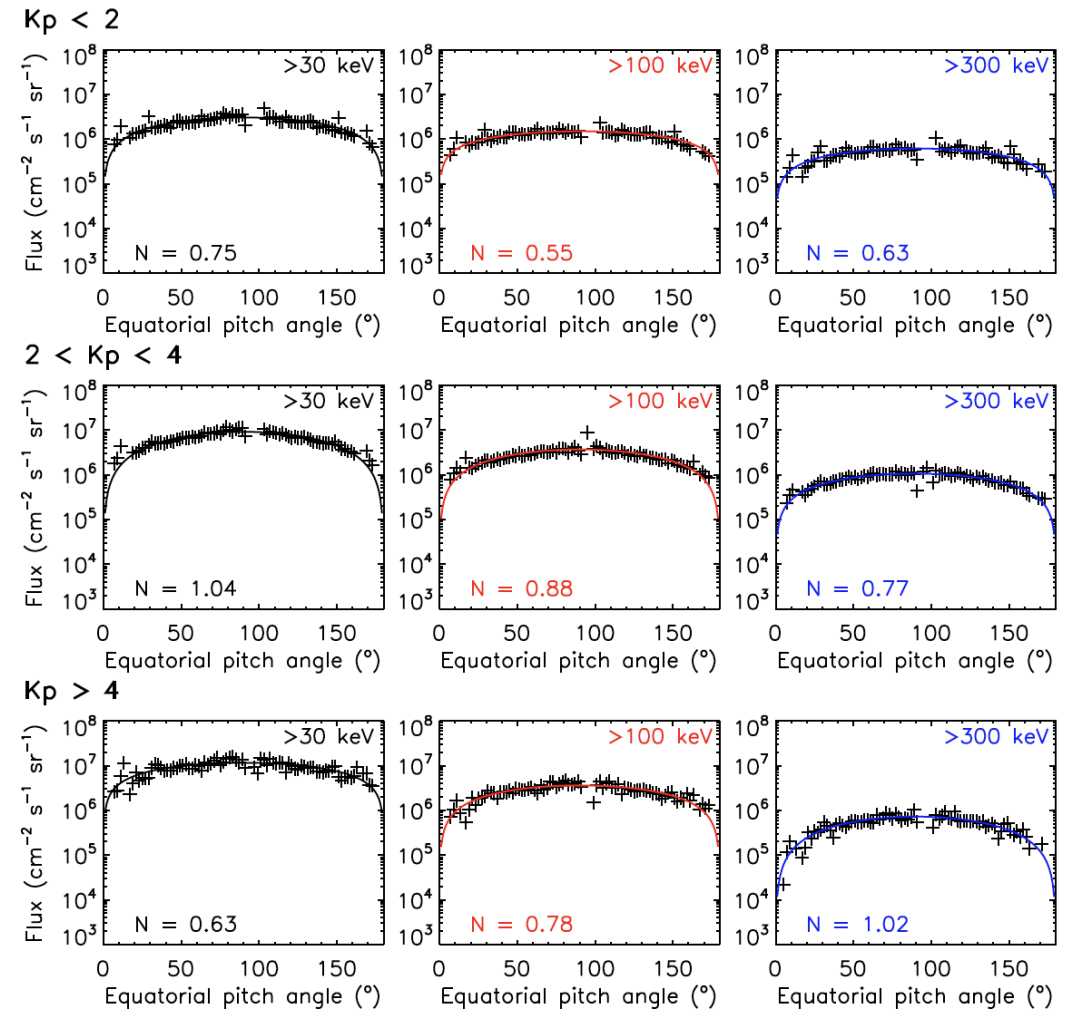
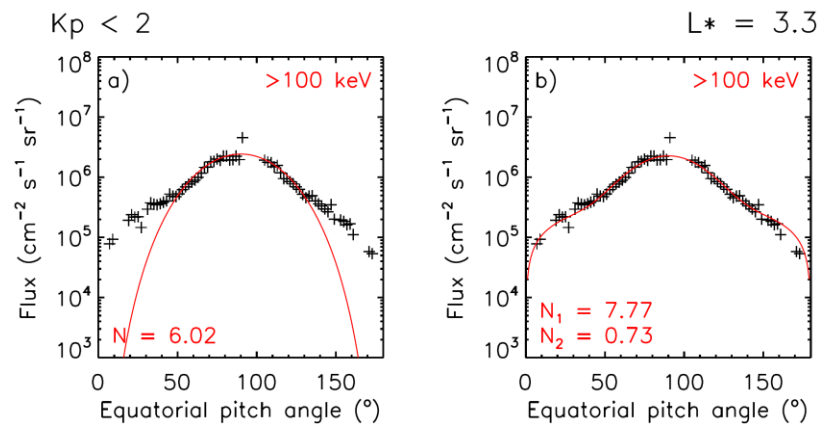


- Assume: integral flux measured = flux at the magnetic equator with a pitch angle given by conservation of μ
- Assume an equatorial pitch angle distribution for the integral flux
- Integrate over this distribution to get omnidirectional flux
- POES measures >30 , >100 , and >300 keV flux – use 3.5 years of MagEIS data to find equatorial pitch angle distributions

Convert to Omnidirectional flux

 $L^* = 4.9$

- $F(E > E_t, \alpha) = F(E > E_t, 90^\circ) \sin^{N(E_0)} \alpha$
- Integrate the MagEIS data
- Find equatorial pitch angles of the MagEIS pitch angle bins
- Sort by Kp and L^*



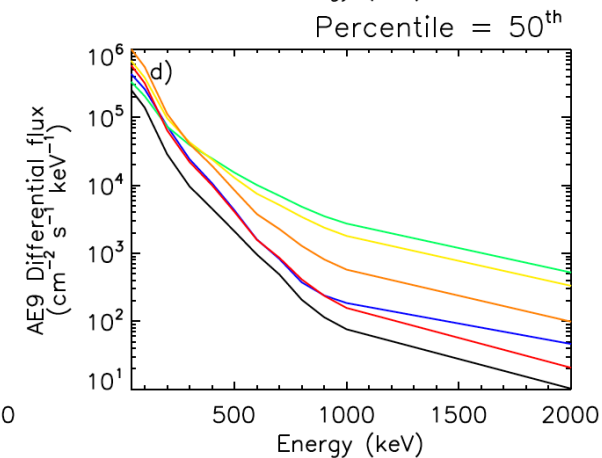
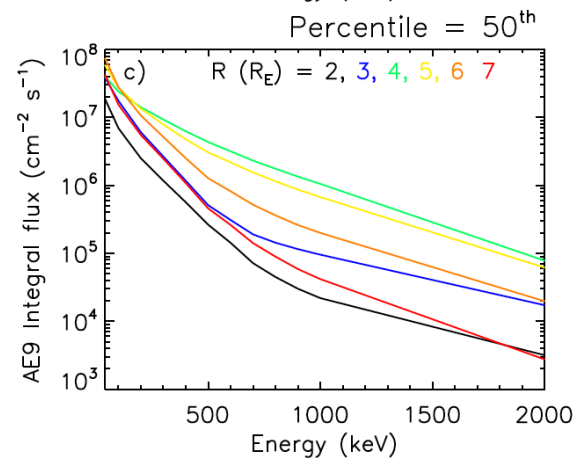
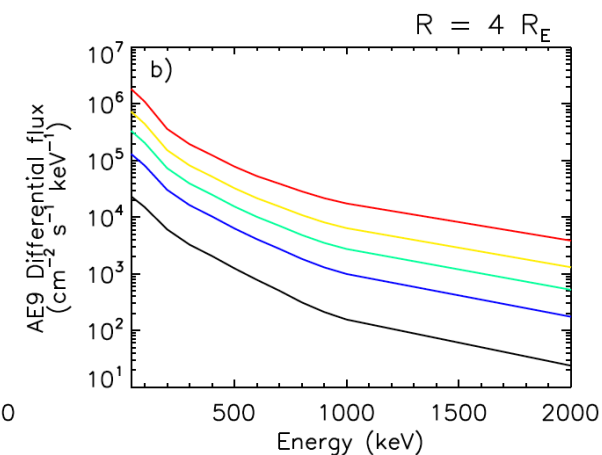
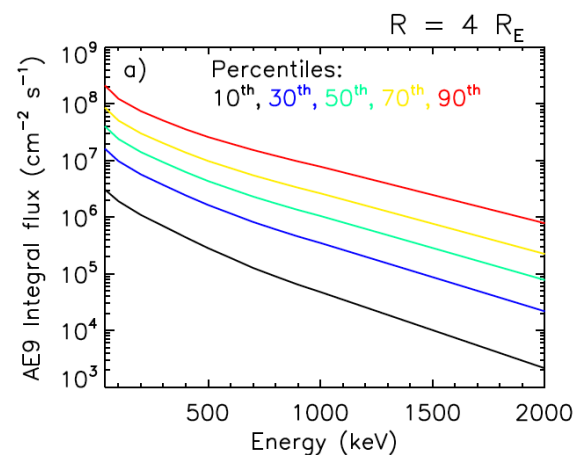
$$F(E > E_t, \alpha) = AF(E > E_t, 90^\circ) \sin^{N_1(E_0)} \alpha + (1 - A)F(E > E_t, 90^\circ) \sin^{N_2(E_0)} \alpha$$

Use integral data to infer differential flux

-Two methods explored

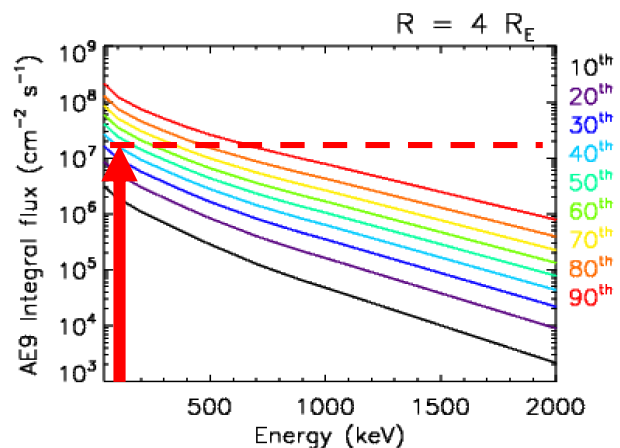
1) AE9 distributions method

- Use integral and differential flux distributions from the IRENE AE9 model
- For flux measured at a certain L^* we take the flux-energy distributions at distances: $(L^* - 1 R_E) < R < (L^* + 1 R_E)$

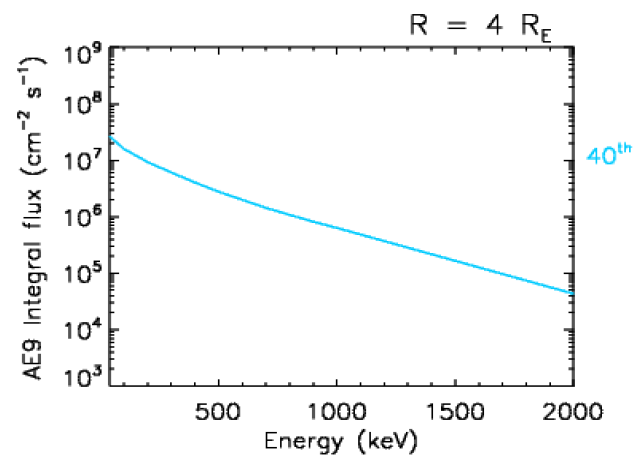


AE9 distributions method

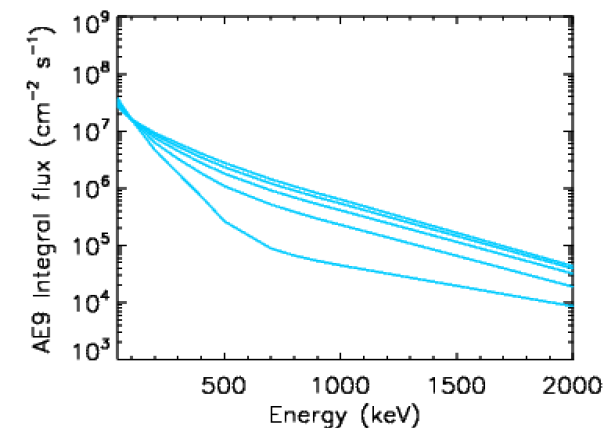
1] Compare the POES >100 keV flux to the AE9 integral flux distributions



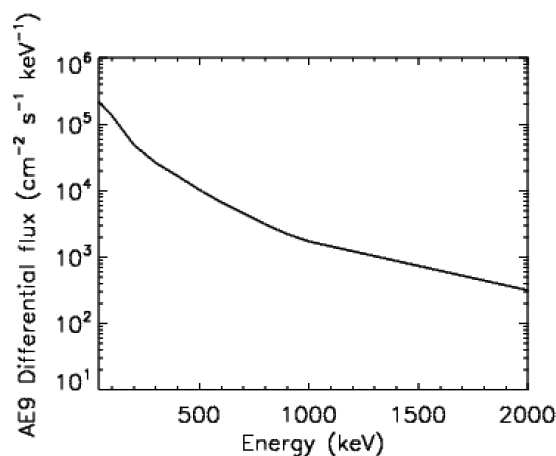
2] Extract distribution closest to data



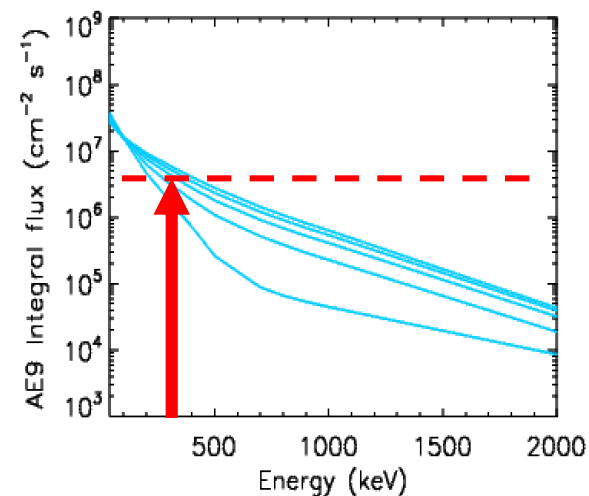
3] Repeat for other distances in range



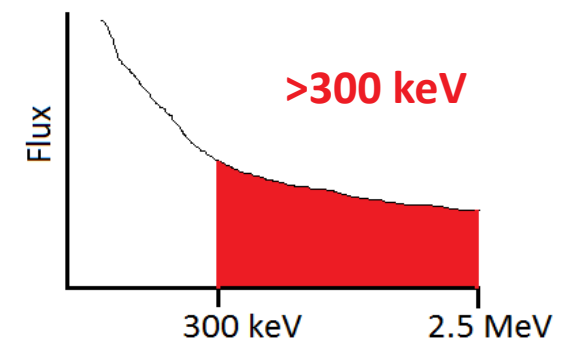
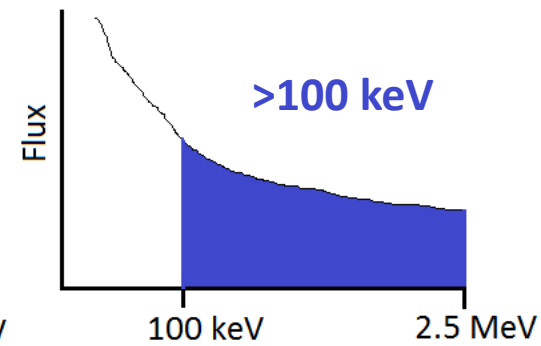
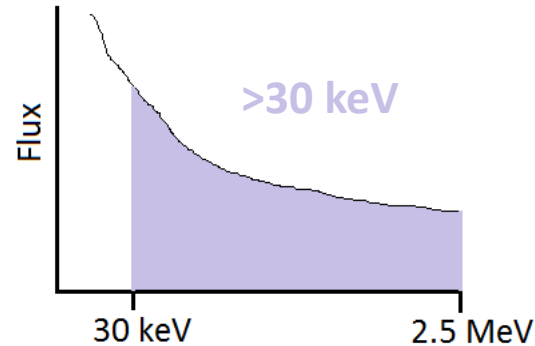
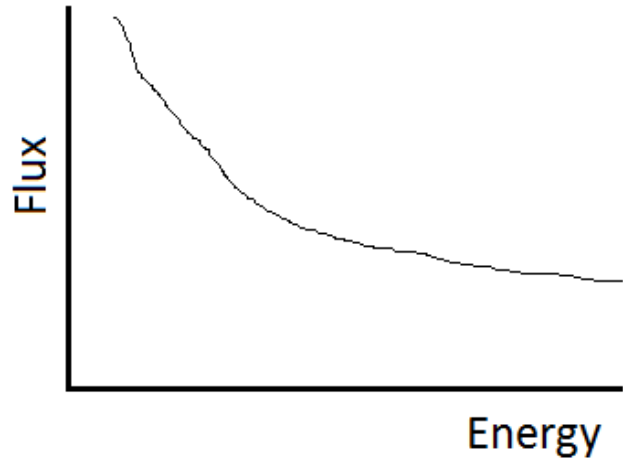
5] Use the equivalent differential flux distribution



4] Compare POES >300 keV flux



2) Iterative method



- Based on Reverse Monte Carlo
- Start with a distribution
- Calculate the three integrals
- Calculate χ^2
- Move a random point – imposing the constraint that flux must fall with increasing energy
- Recalculate χ^2
- If $\chi^2_{\text{new}} < \chi^2_{\text{old}}$ then accept move, if $\chi^2_{\text{new}} > \chi^2_{\text{old}}$ then accept move with probability $\exp\left(-\frac{\chi^2_{\text{new}} - \chi^2_{\text{old}}}{2}\right)$

$$\chi^2 = \sum \frac{(f_{\text{calc}} - f_{\text{obs}})^2}{\sigma^2}$$

Convert to 90° equatorial pitch angle

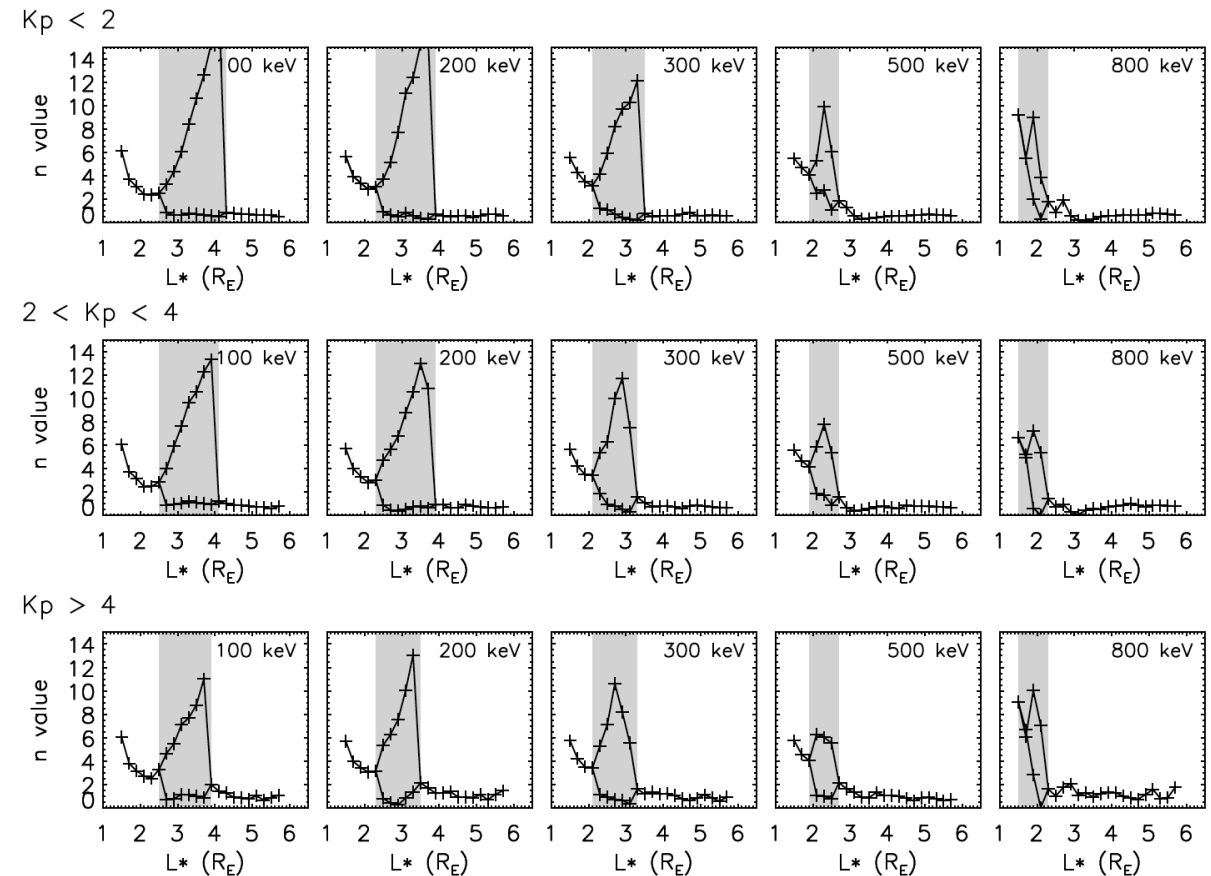
- Have omnidirectional differential flux
- Again need to assume an equatorial pitch angle distribution
- Use average equatorial pitch angle distributions from MagEIS data

Fit either:

$$F(E > E_0, \alpha) = F(E > E_0, 90^\circ) \sin^{N(E_0)} \alpha$$

Or

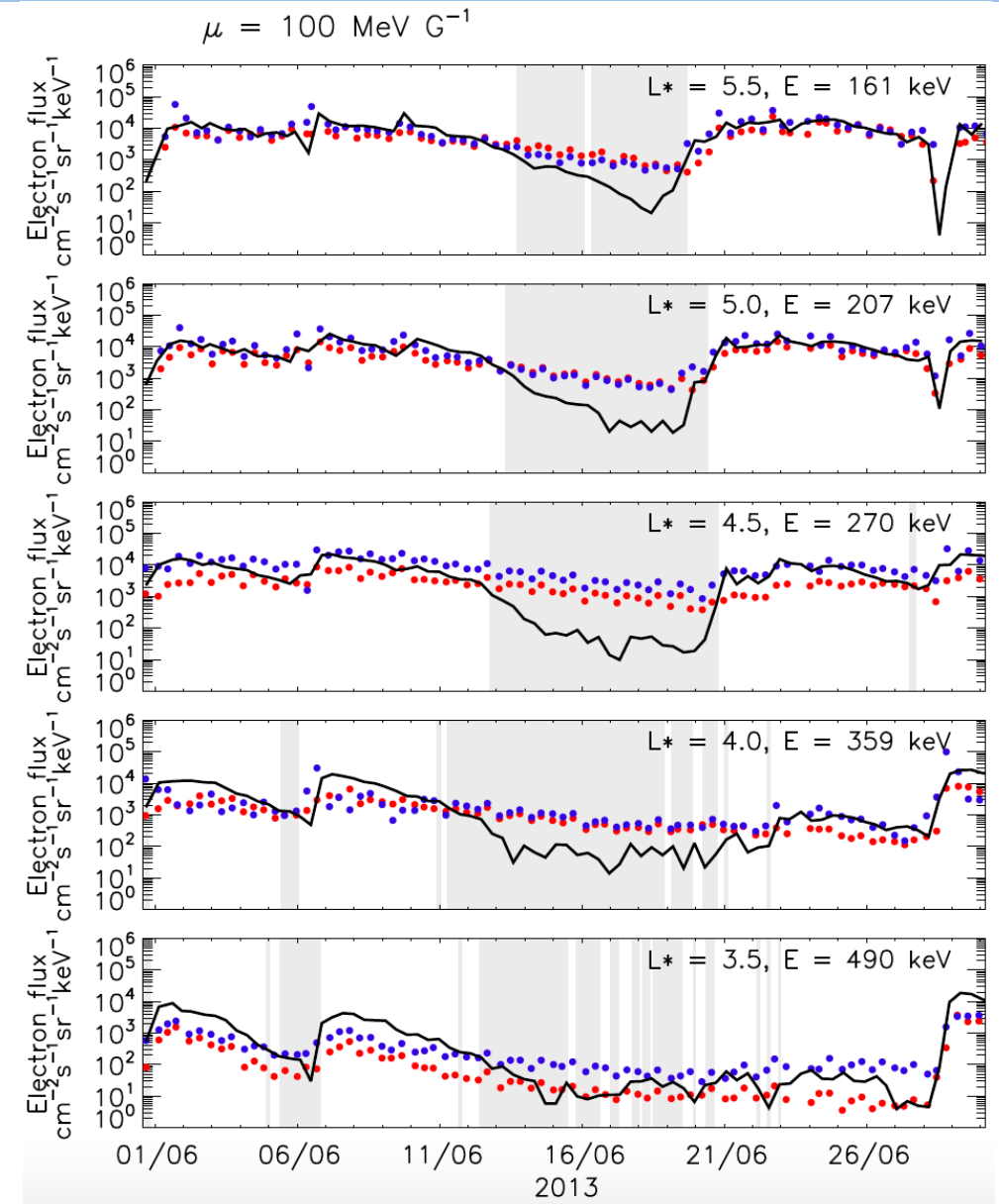
$$F(E > E_0, \alpha) = AF(E > E_0, 90^\circ) \sin^{N_1(E_0)} \alpha + (1 - A)F(E > E_0, 90^\circ) \sin^{N_2(E_0)} \alpha$$



Validation

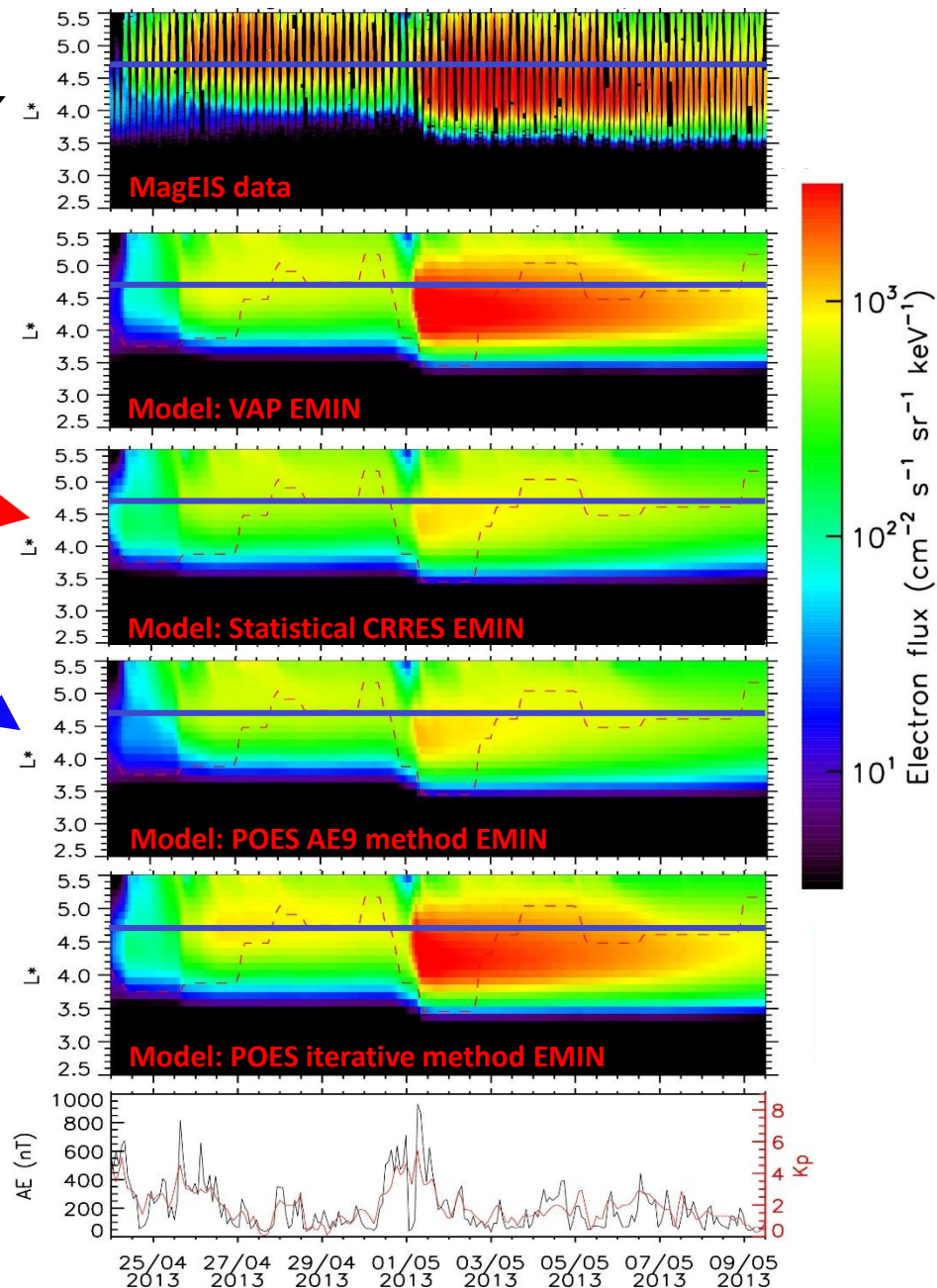
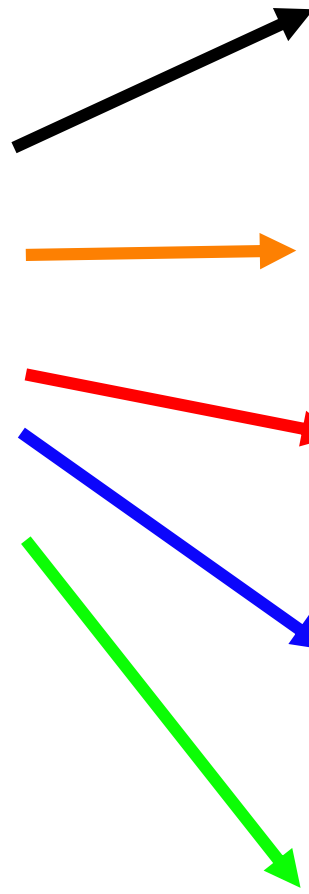
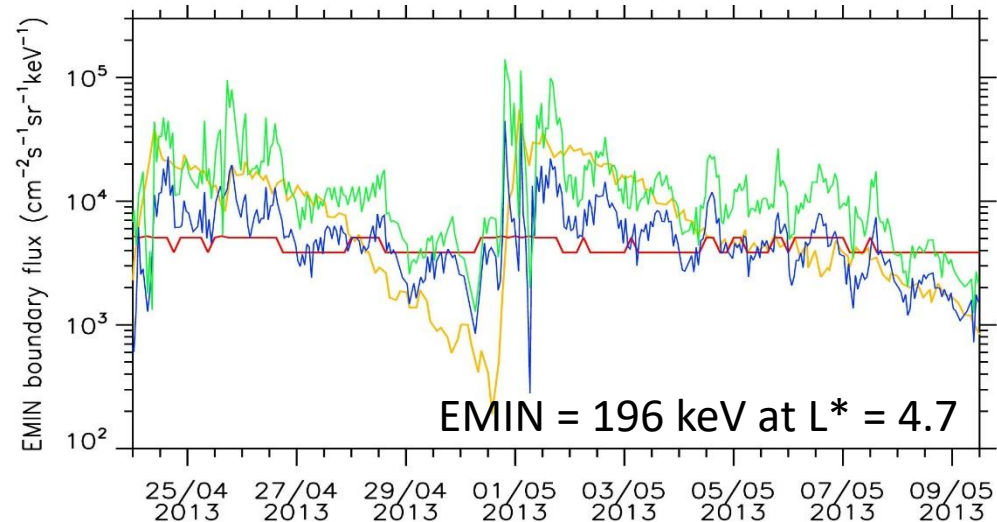
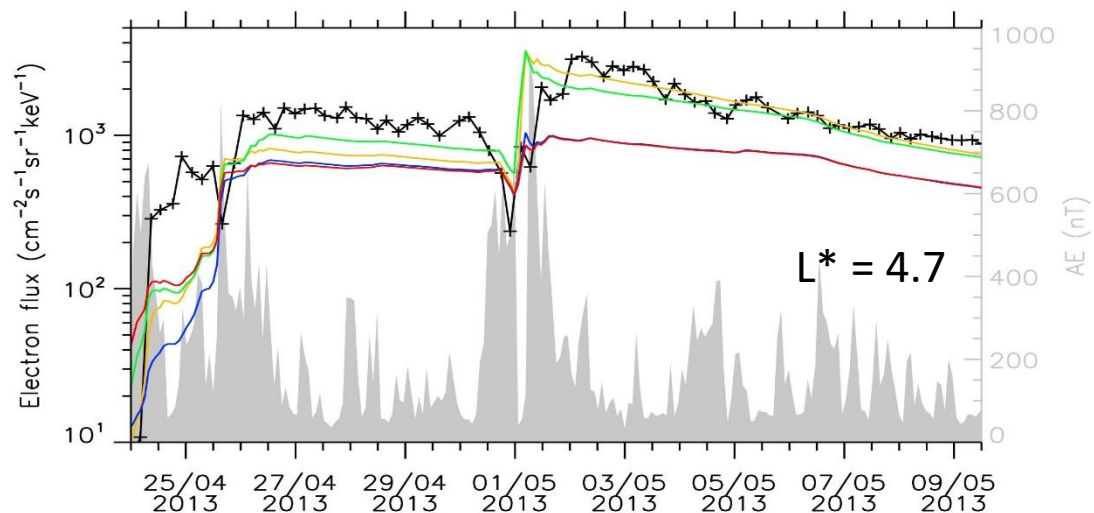
- Follow line of constant $\mu = 100$ MeV/G

Finally, we can use this differential flux data at 90 degree pitch angle to calculate the PSD for the low energy boundary condition.



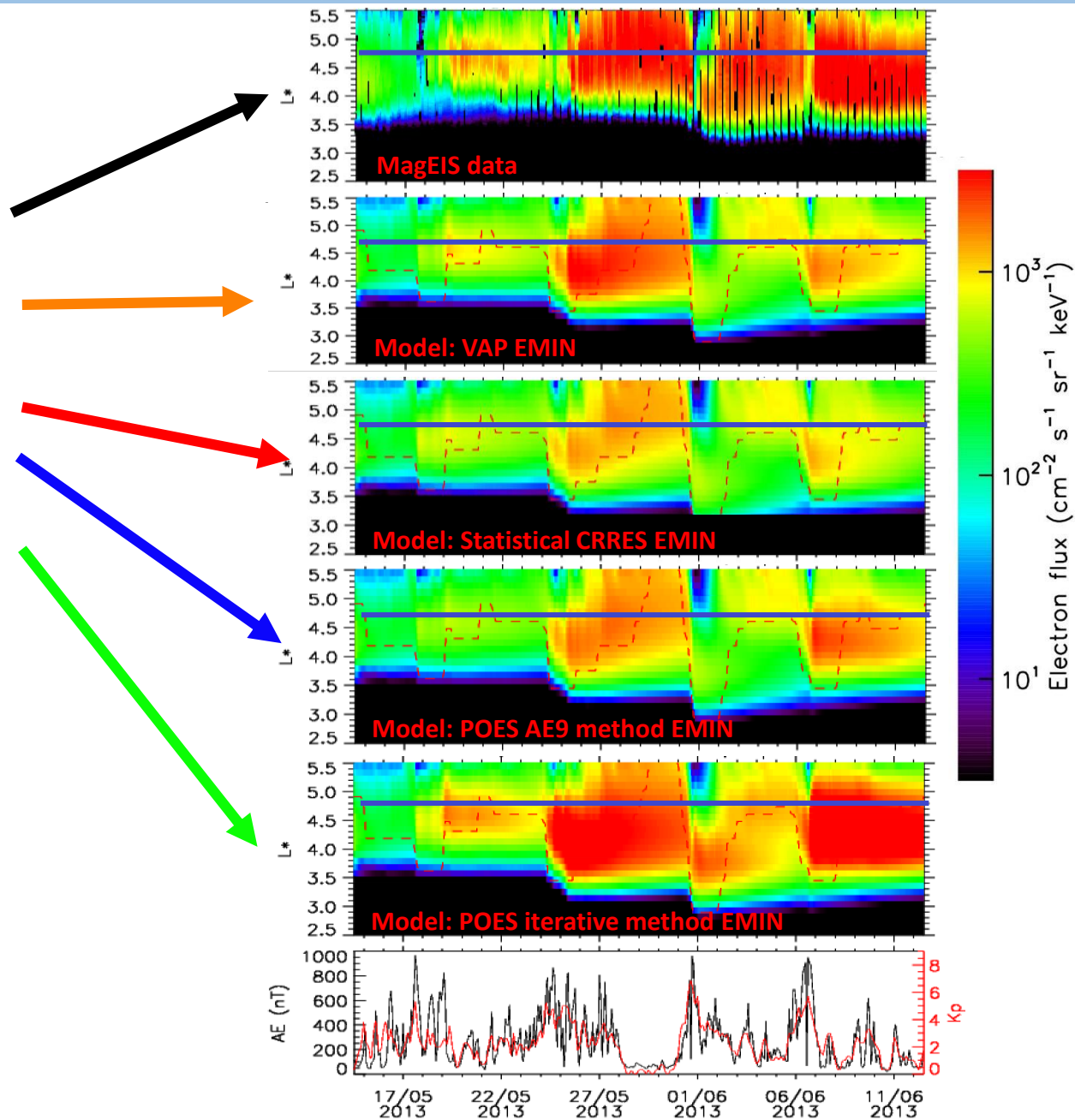
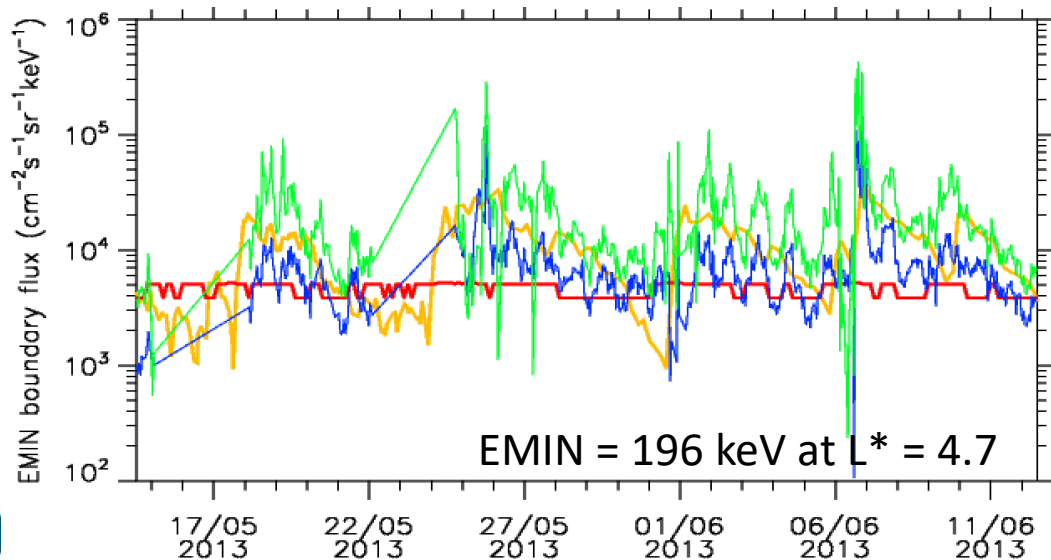
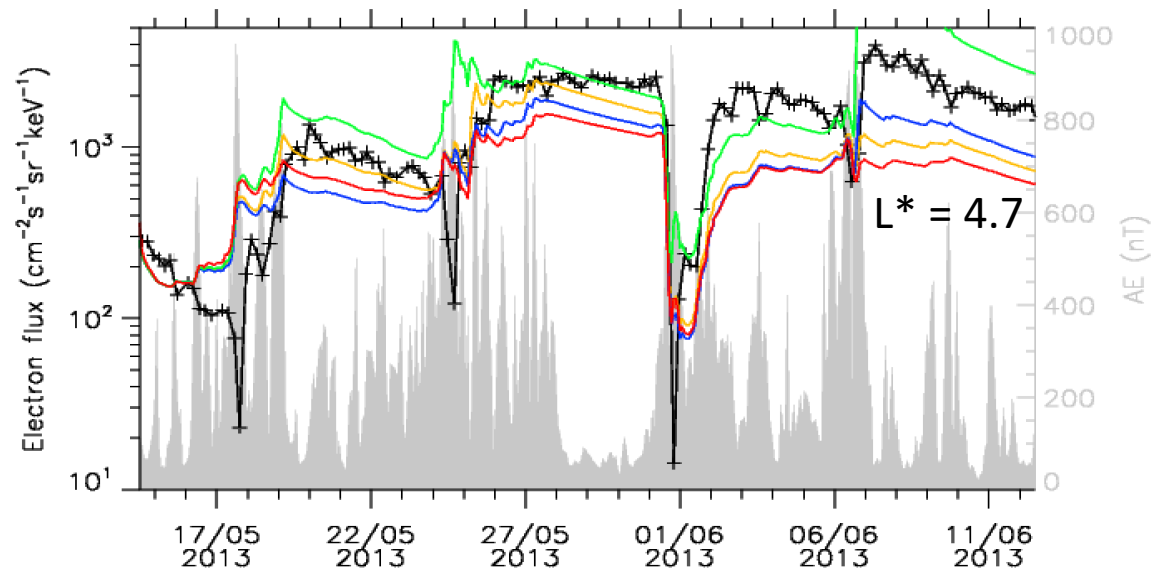
23rd April 2013 – 9th May 2013

1013.01 keV Electron flux, 90° pitch angle



15th May 2013 – 12th June 2013

1013.01 keV Electron flux, 90° pitch angle



Conclusions

- Developed a method to generate event specific low energy boundary conditions from POES MEPED data
 - Useful when Van Allen Probes data is not available
 - High time resolution
- Using the POES generated low energy boundary performed better than the statistical model formed from CRRES data
- Varying the EMIN boundary condition resulted in variations in the ~1 MeV model output
- Examining variations in the low energy flux could improve our understanding of acceleration events